



**NANYANG  
TECHNOLOGICAL  
UNIVERSITY**  
SINGAPORE



# Improving Speed of Dilithium's Signing Procedure

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- 1 Context
- 2 Background
- 3 Algorithmic Optimizations
- 4 Experimental Results
- 5 Future Work
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- NIST process for standardization of Post-Quantum cryptography is underway.
- Lattice-based cryptography has contributed the maximum number of proposals in terms of post-quantum key exchange and post-quantum signature schemes.



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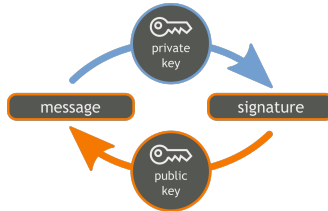
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- We attempt to improve the signing speed through algorithmic optimizations.

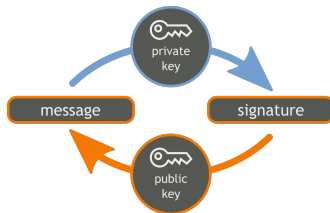
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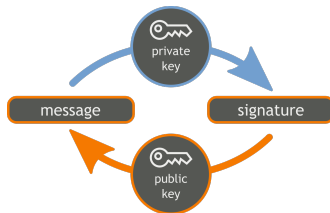
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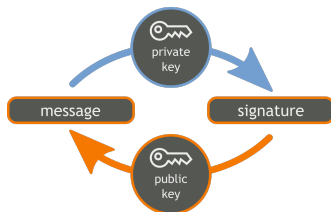


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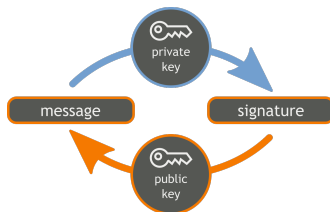
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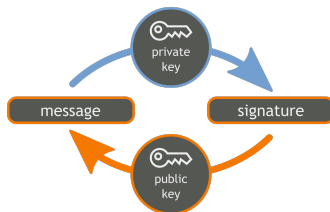
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# Learning With Errors (LWE) Problem



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- Module LWE:  $\mathbf{R}_q^{k \times l} = (\mathbb{Z}_q[X]/(X^n + 1))^{k \times l}$  with  $\mathbf{A} \in \mathbf{R}_q^{k \times \ell}$ ,  $\mathbf{S} \in \mathbf{R}_q^\ell$ ,  $\mathbf{E} \in \mathbf{R}_q^k$ .

# Dilithium Signature Scheme

- Security of Dilithium is based on the MLWE problem.
- Computations are performed over *matrices* and *vectors* of polynomials.
- Signature generation is an iterative procedure with multiple rejection conditions.
- Two algorithmic level optimizations to improve signing speed have been explored.
  - *Opt-1*: Reduction of computations in every rejected iteration.
  - *Opt-2*: Reduction of repetition rate.

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- Is it possible to detect the rejections early to reduce the overhead of the rejected iterations?
- We perform an *early-evaluation* of the rejection conditions, so we detect the rejections early and immediately abort the current iteration.



# Dilithium's Signing Procedure

```

1 Procedure Sign( $sk, M$ )
2    $\mathbf{A} \in R_q^{k \times \ell} := \text{ExpandA}(\rho)$ 
3    $\mu = \text{CRH}(\text{tr}\|M)$ 
4    $\kappa = 0, (\mathbf{z}, \mathbf{h}) = \perp$ 
5   while  $(\mathbf{z}, \mathbf{h}) = \perp$  do
6      $\mathbf{y} \in S_{\gamma_1-1}^\ell := \text{ExpandMask}(K\|\mu\|\kappa)$ 
7      $\mathbf{w} = \mathbf{A} \cdot \mathbf{y}$ 
8      $\mathbf{w}_1 = \text{HB}_q(\mathbf{w}, 2\gamma_2)$ 
9      $\mathbf{c} \in B_{60} = H(\mu\|\mathbf{w}_1)$ 
10     $\mathbf{z} = \mathbf{y} + \mathbf{c} \cdot \mathbf{s}_1$ 
11     $(\mathbf{r}_1, \mathbf{r}_0) := \text{D}_q(\mathbf{w} - \mathbf{c} \cdot \mathbf{s}_2, 2\gamma_2)$ 
12    if  $\|\mathbf{z}\|_\infty \geq \gamma_1 - \beta$  or  $\|\mathbf{r}_0\|_\infty \geq \gamma_2 - \beta$  or
13        $\mathbf{r}_1 \neq \mathbf{w}_1$  then
14       |  $(\mathbf{z}, \mathbf{h}) = \perp$ 
15     else
16       |  $\mathbf{h} = \text{MH}_q(-\mathbf{c} \cdot \mathbf{t}_0, \mathbf{w} - \mathbf{c} \cdot \mathbf{s}_2 + \mathbf{c} \cdot \mathbf{t}_0, 2\gamma_2)$ 
17       | if  $\|\mathbf{c} \cdot \mathbf{t}_0\|_\infty \geq \gamma_2$  or  $\text{wt}(\mathbf{h}) > \omega$  then
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20     $\kappa = \kappa + 1$ 
21  end
22  return  $\sigma = (\mathbf{z}, \mathbf{h}, \mathbf{c})$ 

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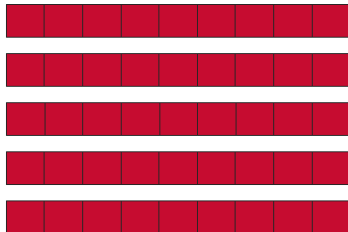
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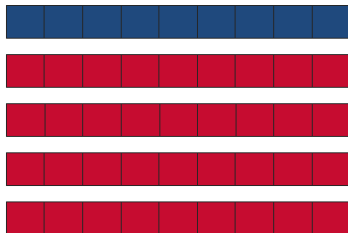
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- The condition has to be satisfied for all coefficients of a given module.
- Consider the computations involving module  $\mathbf{z} \in R_q^\ell$ .

# Evaluation of Rejection Conditions



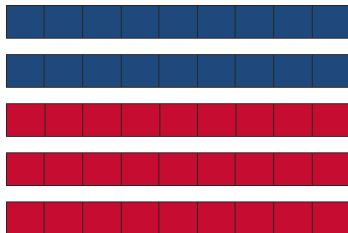
# Evaluation of Rejection Conditions



No of Computations: 1

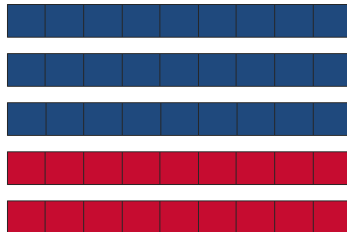


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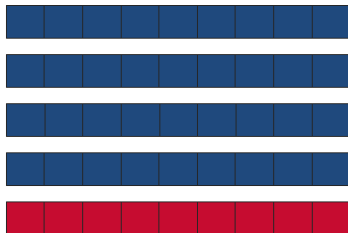
No of Computations: 2

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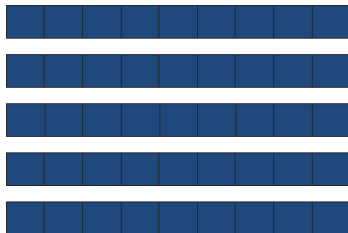
No of Computations: 3

# Evaluation of Rejection Conditions



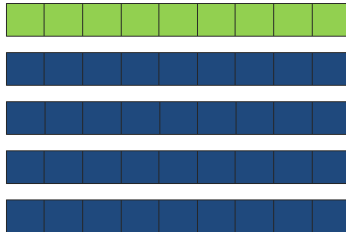
No of Computations: 4

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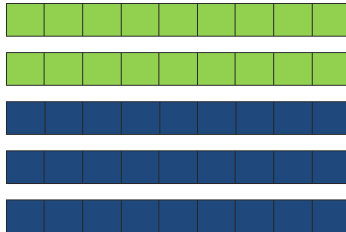
No of Computations:  $N$

# Evaluation of Rejection Conditions



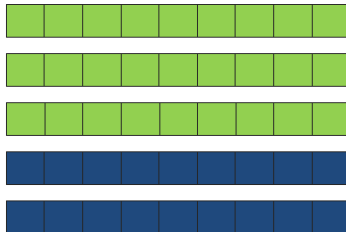
No of Computations:  $N+1$

# Evaluation of Rejection Conditions



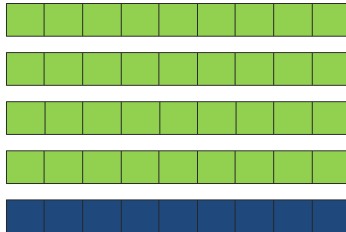
No of Computations:  $N+2$

# Evaluation of Rejection Conditions



No of Computations:  $N+3$

# Evaluation of Rejection Conditions



No of Computations:  $N+4$

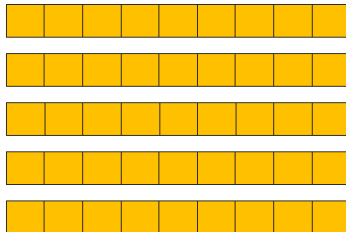


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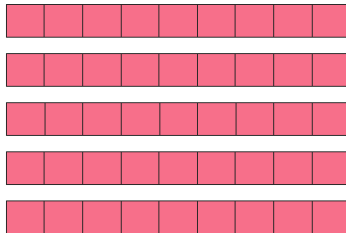
No of Computations:  $2N$

# Evaluation of Rejection Conditions



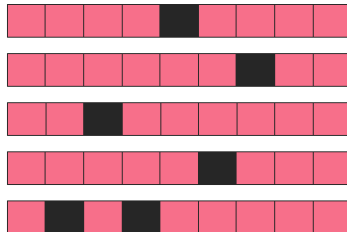
No of Computations:  $3N$

# Evaluation of Rejection Conditions



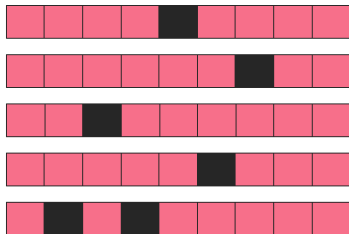
No of Computations:  $C*N$

# Evaluation of Rejection Conditions



Checking defective elements:

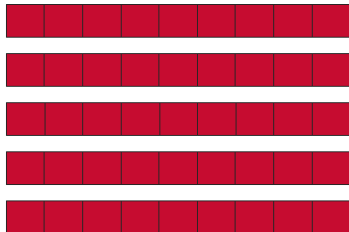
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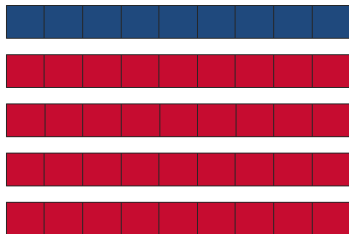
If (number of black boxes  $> 0$ )  
Reject

**Total Computations to  
compute rejection: :  $(C+1)*N$   
condition**

## *Early Evaluation of Rejection Conditions*



## *Early Evaluation* of Rejection Conditions



No of Computations: 1

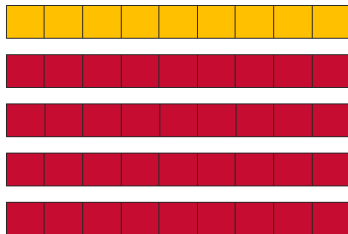
## *Early Evaluation* of Rejection Conditions



No of Computations: 2

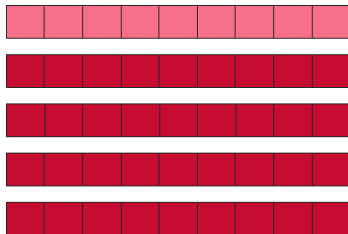


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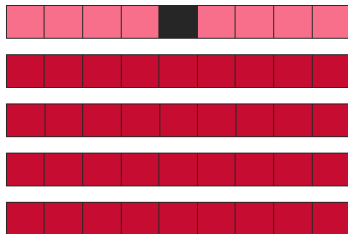
No of Computations: 3

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No of Computations:  $C$

## *Early Evaluation of Rejection Conditions*



No of Computations:  $C+1$

**Rejection done with only  
( $C+1$ ) computations**

## Early Evaluation of Rejection Conditions

- We perform the complete set of computations **one polynomial at a time**.
- **Best Case** -  $(C+1)$  computations.
- **Worst Case** -  $((C+1)*N)$  computations.
- **Average Case** -  $((C+1)*\frac{N}{2})$  computations.
- We apply the same optimization to all the *Infy\_Checks* in Dilithium's signing procedure.

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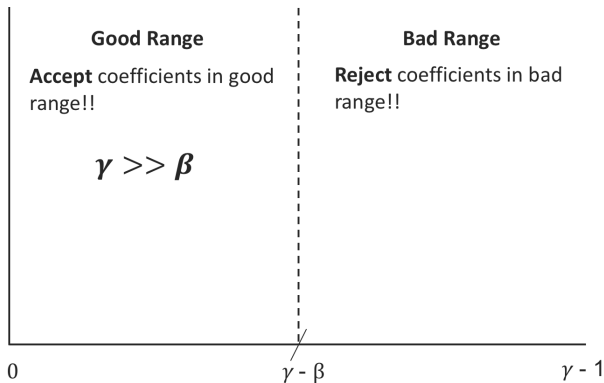
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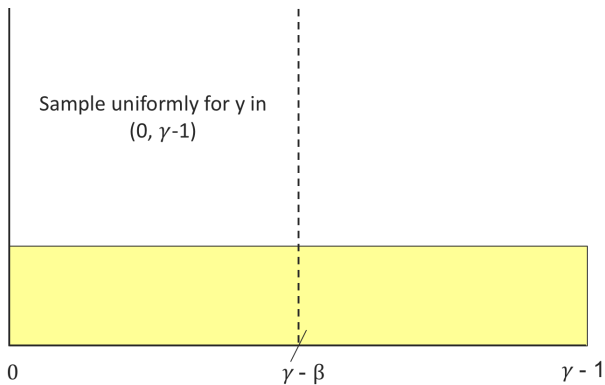
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- Coefficients of  $\mathbf{y}$  are uniformly distributed in  $[0, \gamma_1 - 1]$ .
- Coefficients of  $\mathbf{sc}$  are very small and normally distributed in  $[0, \beta]$ .

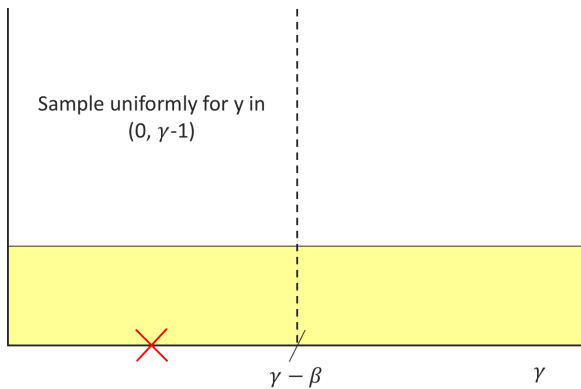
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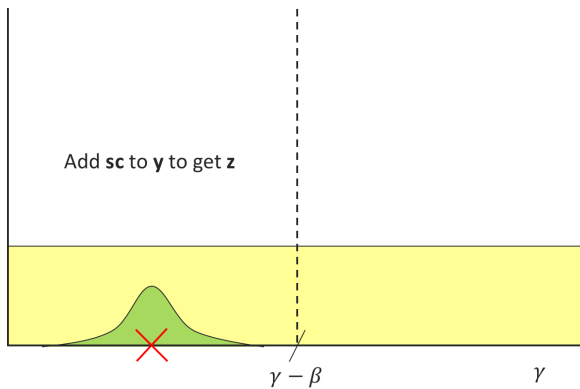
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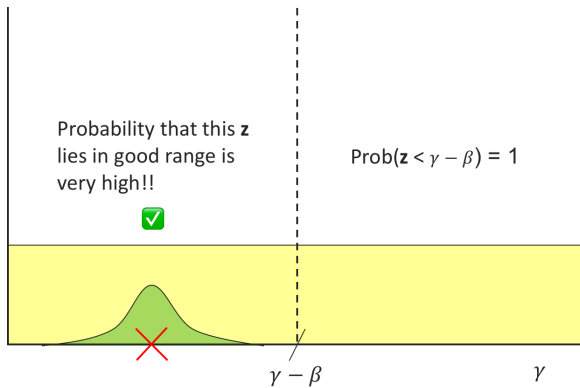
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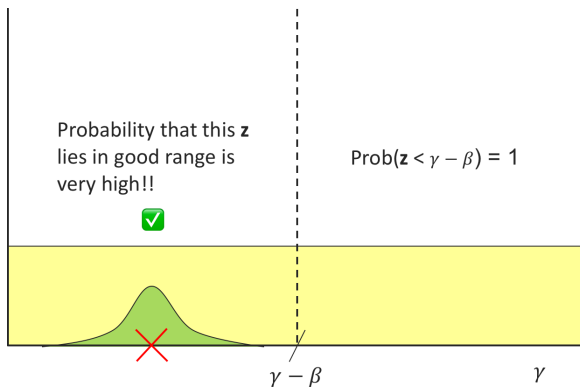
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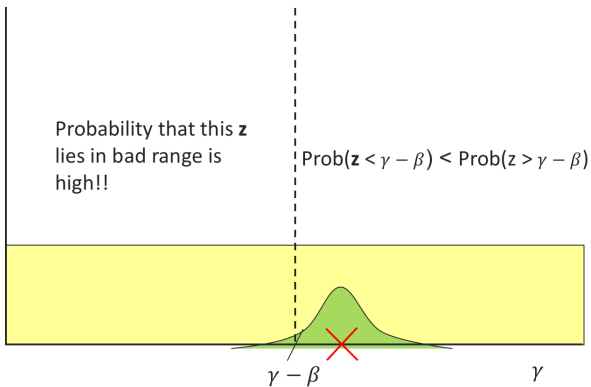


## Generation of $z$

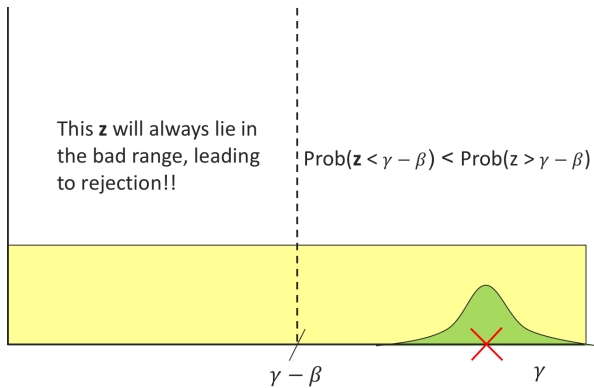




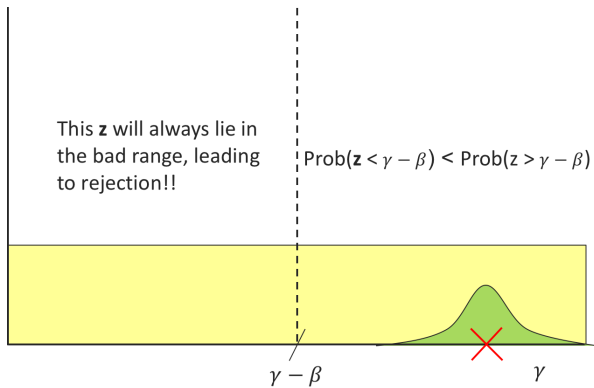
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## Improving the Repetition Rate

- Rejection Sampling is performed so as to hide the  $sc$  component within  $\mathbf{z}$ .
- Allows to generate upto  $2^{80}$  signatures without leaking the distribution of the  $sc$  component.

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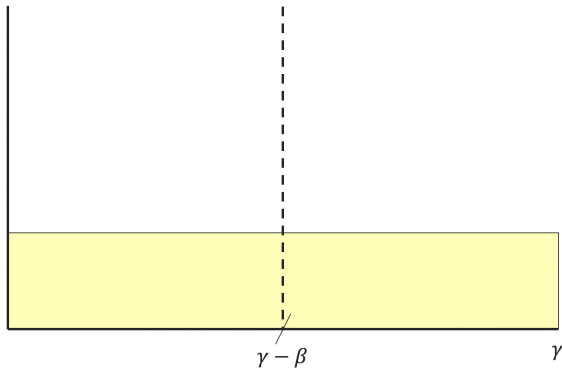
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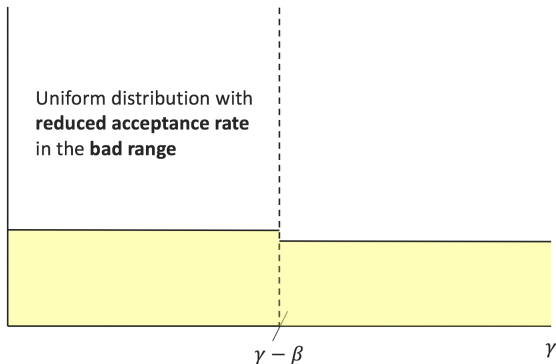
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- $\mathbf{y}$  is sampled uniformly in  $[0, \gamma_1]$  and hence has a certain non-negligible probability that its corresponding  $\mathbf{z}$  lies in the bad range.
- Can we alter the distribution of  $\mathbf{y}$  so as to reduce the occurrence of  $\mathbf{z}$  in the bad range?

# Uniform Distribution with Reduced Acceptance Rate

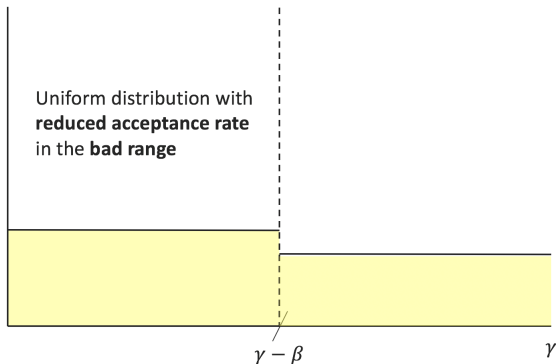




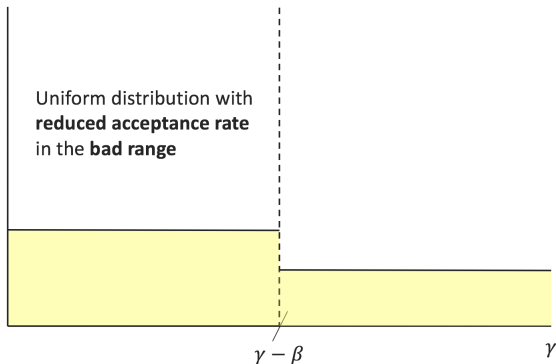
# Uniform Distribution with Reduced Acceptance Rate



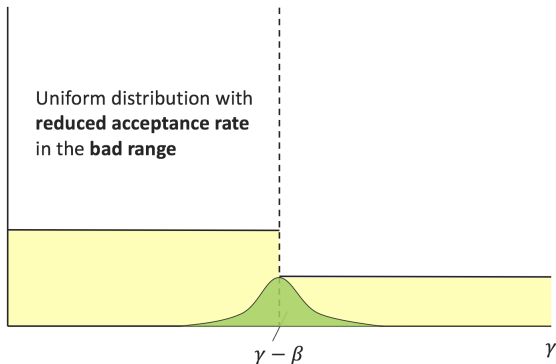
# Uniform Distribution with Reduced Acceptance Rate



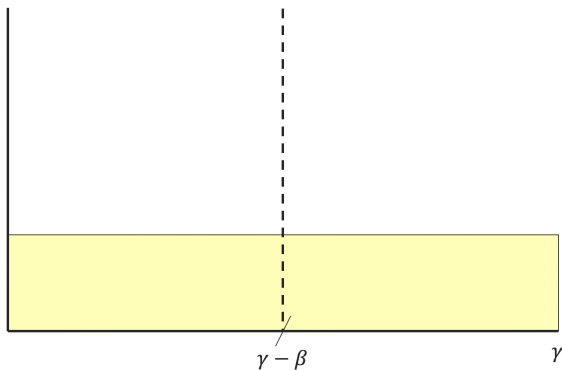
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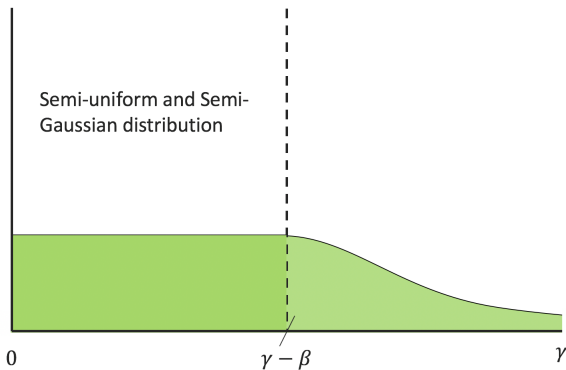
# Uniform Distribution with Reduced Acceptance Rate



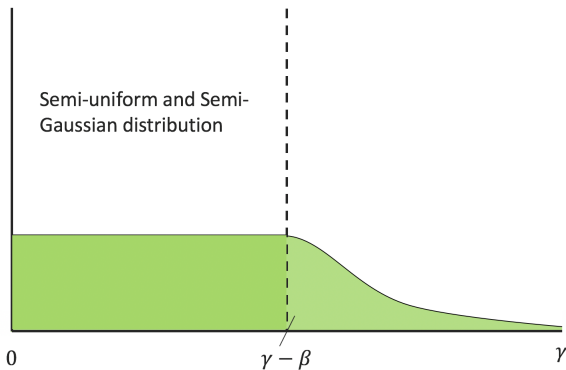
## Semi-Uniform and Semi-Gaussian



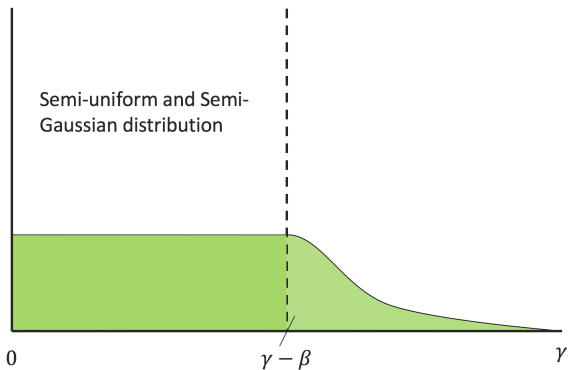
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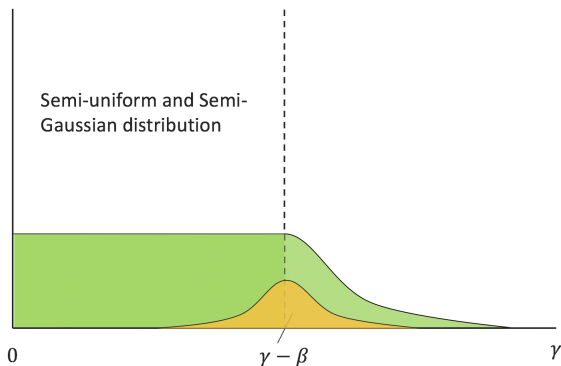


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# Semi-Uniform and Semi-Gaussian



# Alternate Distributions for Sampling $y$

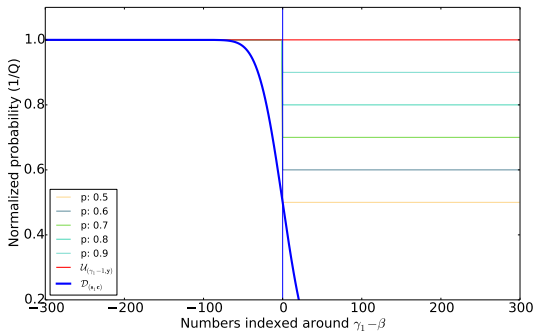


Figure:  $\mathcal{U}_{(\gamma_1 - \beta, \gamma_1 - 1, p)}$  - Uniform distribution with reduced acceptance rate  $p$

# Alternate Distributions for Sampling $y$

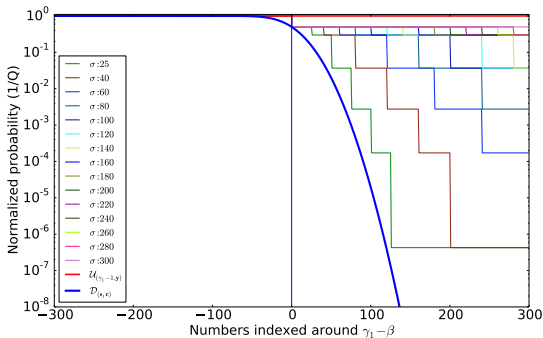


Figure:  $\mathcal{D}_{(\gamma_1 - \beta, \gamma_1 - 1, \sigma)}$  - Piece-wise Gaussian distribution with standard deviation  $\sigma$

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## Experimental Results

- Implementation of *Early-Eval* optimization and *Improved-Sampling* optimizations on reference implementation of Dilithium.
- Both the optimizations can be employed independently.
- Since both optimizations are done at the algorithmic level, they can be ported to all implementation platforms.
- Results were obtained for about  $10^7$  runs of the signing procedure.
- Implemented on Intel(R) Core(TM) i5-4460 CPU 3.20GHz and compiled with gcc-4.2.1.

# Experimental Results

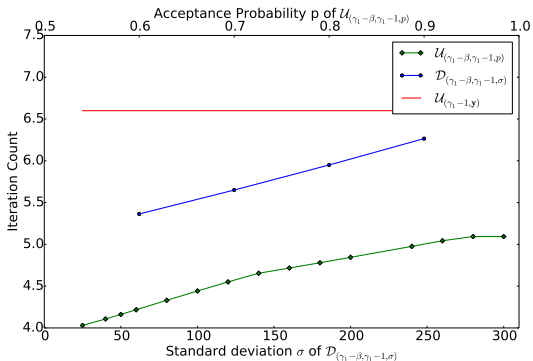


Figure: Improvements in iteration Count evaluated for various parameters of our alternate distributions

# Experimental Results

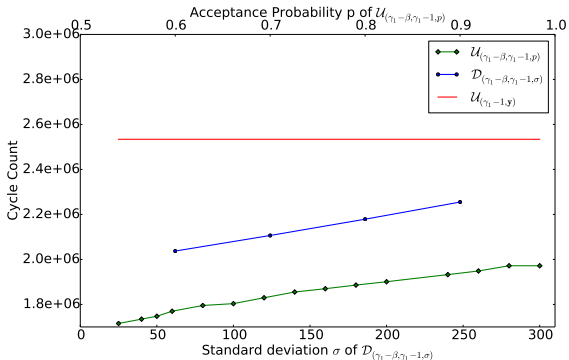


Figure: Improvements in Cycle count evaluated for various parameters of our alternate distributions

## Experimental Results

- *Early-Eval* optimization yields improvement of about 8% in the signing speed.
- Combination of *Early-Eval* and *Improved-Sampling* optimizations could yield speed up upto 38%.
- *Early-Eval* optimization does not have any impact on security of the scheme.
- Does the use of improved distributions for  $y$  affect the security of the scheme? If so, by how much?
- How many signatures does the attacker need to observe an exploitable skew in the distribution of  $z$ .
- This could lead to a potential quantitative trade-off between security and efficiency, which needs to be evaluated.



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## Future Work

- Security Analysis of the signing procedure with improved distribution.
- Evaluation of the security-efficiency trade-off due to use of improved distributions.
- Utilization of a constant-time Gaussian sampler to sample from the improved distribution.

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## Future Work

- This work proposes algorithmic optimizations for the Dilithium signature scheme
- We propose two optimizations:
  - *Early-Eval* optimization
  - *Improved-Sampling* optimization
- We were able to achieve a speed-up of upto 38% by employing a combination of both the optimizations.
- Incorporation of the *Improved-Sampling* optimization could lead to a potential security-efficiency trade-off.
- We intend to perform a quantitative evaluation of the security-efficiency trade-off as part of future work.

Thank you!  
Any questions?

